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Concept map

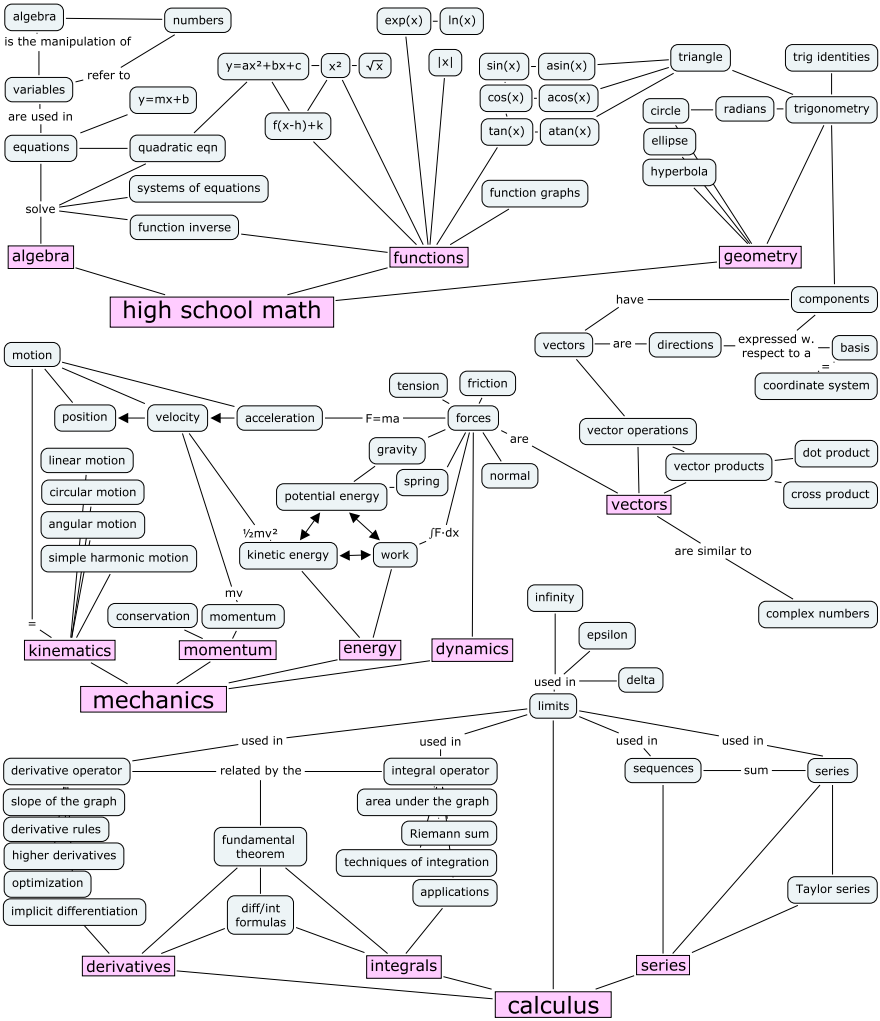

Figure 1: Each concept in this diagram corresponds to one section in the book.

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by Ivan Savov

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